

$$Y = \begin{cases} 0 & \text{cured} \\ 1 & \text{not cured} \end{cases}$$

T : survival time.

model:

$$P(T > t | Y=1) = e^{-(\lambda t)^\gamma}$$

$$P(T > t | Y=0, a) = \frac{S_0(a+t)}{S_0(a)}$$

age at entry



$$P(Y=0 | x) = \frac{1}{1 + e^{\alpha + \beta x}}$$

covariate

$$P(Y=1 | x) = \frac{e^{\alpha + \beta x}}{1 + e^{\alpha + \beta x}}$$

Data: $(t, \delta, x, a, \underline{y})$.

t, δ, x, a are as before.

$$y = \begin{cases} 0 & \text{cured} \\ 1 & \text{not cured} \end{cases}$$

$\delta=0$ censored

$\delta=1$ uncensored dead.

The observation y could be missing.

The observation y is not equal to 0.

If $y=1$ (died due to the disease)

the likelihood is:

$$L = \frac{e^{\alpha + \beta x}}{1 + e^{\alpha + \beta x}} \cdot \underbrace{e^{-(\lambda t)^\gamma}}_{\text{Weibull}} \cdot \underbrace{\left[\lambda \gamma (\lambda t)^{\gamma-1} \right]}_{\substack{\delta=1 \\ \delta=0}}$$

$\boxed{\delta=1}$

If $y = 0$ the likelihood is

$$L = \left[\underbrace{\frac{1}{1 + e^{\alpha + \beta x}} \frac{S_0(a+t)}{S_0(a)}}_{\text{cured}} + \underbrace{\frac{e^{\alpha + \beta x}}{1 + e^{\alpha + \beta x}} e^{-(\lambda x)^{\gamma}}}_{\text{not cured}} \right]^{1 - \int_0^t \delta}$$

survival

$$\left[\underbrace{\frac{1}{1 + e^{\alpha + \beta x}} f_0(a+t)}_{\text{density}} + \frac{e^{\alpha + \beta x}}{1 + e^{\alpha + \beta x}} \lambda \gamma (\lambda x)^{\gamma-1} e^{-(\lambda x)^{\gamma}} \right]^{\delta}$$

dead

cured

↓
not cured

or 0.6%

$$P(0 < X < 1 \mid X \geq 0)$$

$$P(1 < X < 2 \mid X \geq 1)$$

$$P(X < 2) = \underbrace{P(1 < X < 2 \mid X \geq 1)} \cdot \underline{\underline{P(X \geq 1)}}$$